

Case 2:

$$\begin{aligned}
 s(t) &= \frac{2}{5} - \frac{41}{2500}t + \frac{991}{2500000}t^2 - \frac{265369}{3750000000}t^3 + \frac{50195873}{7500000000000}t^4 + O(t^5). \\
 e(t) &= \frac{1}{5} + \frac{18}{625}t + \frac{1013}{2500000}t^2 + \frac{273323}{3750000000}t^3 - \frac{41249251}{7500000000000}t^4 + O(t^5). \\
 i(t) &= \frac{1}{10} - \frac{9}{2500}t + \frac{1161}{625000}t^2 - \frac{243703}{1875000000}t^3 + \frac{34601071}{3750000000000}t^4 + O(t^5). \\
 r(t) &= \frac{3}{10} + \frac{17}{500}t - \frac{61}{31250}t^2 + \frac{14227}{9370000}t^3 - \frac{3128621}{3750000000000}t^4 + O(t^5).
 \end{aligned}$$

Case 3:

$$\begin{aligned}
 s(t) &= \frac{2}{5} + \frac{9}{2500}t - \frac{3159}{2500000}t^2 - \frac{37173}{1250000000}t^3 + \frac{7995141}{2500000000000}t^4 + O(t^5). \\
 e(t) &= \frac{1}{5} + \frac{18}{625}t + \frac{2763}{2500000}t^2 + \frac{106191}{1250000000}t^3 - \frac{6079167}{2500000000000}t^4 + O(t^5). \\
 i(t) &= \frac{1}{10} - \frac{9}{2500}t + \frac{1161}{625000}t^2 - \frac{66651}{625000000}t^3 + \frac{10219107}{12500000000000}t^4 + O(t^5). \\
 r(t) &= \frac{3}{10} + \frac{7}{500}t - \frac{119}{125000}t^2 + \frac{5551}{46875000}t^3 - \frac{2509871}{3750000000000}t^4 + O(t^5).
 \end{aligned}$$

Case 4:

$$\begin{aligned}
 s(t) &= \frac{2}{5} + \frac{59}{2500}t - \frac{7309}{2500000}t^2 + \frac{42331}{3750000000}t^3 - \frac{12725027}{7500000000000}t^4 + O(t^5). \\
 e(t) &= \frac{1}{5} + \frac{18}{625}t + \frac{4513}{2500000}t^2 + \frac{363823}{3750000000}t^3 + \frac{15274249}{7500000000000}t^4 + O(t^5). \\
 i(t) &= \frac{1}{10} - \frac{9}{2500}t + \frac{1161}{625000}t^2 - \frac{156203}{1875000000}t^3 + \frac{26713571}{37500000000000}t^4 + O(t^5). \\
 r(t) &= \frac{3}{10} - \frac{3}{500}t + \frac{3}{62500}t^2 + \frac{2659}{31250000}t^3 - \frac{1891121}{3750000000000}t^4 + O(t^5).
 \end{aligned}$$

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